

ТАБЛИЦЯ ПОХІДНИХ

	Елементарних функцій	Складених функцій
1.	$(c)' = 0$	$u = \varphi(x)$
2.	$(x^\alpha)' = \alpha x^{\alpha-1}$	$(u^\alpha)'_x = \alpha u^{\alpha-1} u'_x$
3.	$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$	$(\sqrt{u})'_x = \frac{u'_x}{2\sqrt{u}}$
4.	$\left(\frac{1}{x}\right)' = -\frac{1}{x^2}$	$\left(\frac{1}{u}\right)'_x = -\frac{u'_x}{u^2}$
5.	$(\sin x)' = \cos x$	$(\sin u)'_x = \cos u \cdot u'_x$
6.	$(\cos x)' = -\sin x$	$(\cos u)'_x = -\sin u \cdot u'_x$
7.	$(tg x)' = \frac{1}{\cos^2 x}$	$(tg u)'_x = \frac{u'_x}{\cos^2 u}$
8.	$(ctg x)' = -\frac{1}{\sin^2 x}$	$(ctg u)'_x = -\frac{u'_x}{\sin^2 u}$
9.	$(a^x)' = a^x \ln a$	$(a^u)'_x = a^u \ln a \cdot u'_x, a > 0, a \neq 1$
10.	$(e^x)' = e^x$	$(e^u)'_x = e^u u'_x$
11.	$(\ln x)' = \frac{1}{x}$	$(\ln u)'_x = \frac{u'_x}{u}$
12.	$(\log_a x)' = \frac{1}{x \ln a}$	$(\log_a u)'_x = \frac{u'_x}{u \ln a}, a > 0, a \neq 1$
13.	$(\arcsin x)'_x = \frac{1}{\sqrt{1-x^2}}$	$(\arcsin u)'_x = \frac{u'_x}{\sqrt{1-u^2}}$
14.	$(\arccos x)'_x = -\frac{1}{\sqrt{1-x^2}}$	$(\arccos u)'_x = -\frac{u'_x}{\sqrt{1-u^2}}$
15.	$(\arctg x)'_x = \frac{1}{1+x^2}$	$(\arctg u)'_x = \frac{u'_x}{1+u^2}$
16.	$(\text{arcctg } x)'_x = -\frac{1}{1+x^2}$	$(\text{arcctg } u)'_x = -\frac{u'_x}{1+u^2}$

ТАБЛИЦЯ ІНТЕГРАЛІВ

$$1. \int x^\alpha dx = \frac{x^{\alpha+1}}{\alpha+1} + C (\alpha \neq -1); \text{ при } \alpha = 0 \text{ имеем } \int dx = x + C .$$

$$2. \int \frac{dx}{x} = \ln|x| + C .$$

$$3. \int \sin x dx = -\cos x + C .$$

$$4. \int \cos x dx = \sin x + C .$$

$$5. \int \frac{dx}{\cos^2 x} = \operatorname{tg} x + C .$$

$$6. \int \frac{dx}{\sin^2 x} = -\operatorname{ctg} x + C .$$

$$7. \int \frac{dx}{\sqrt{1-x^2}} = \arcsin x + C .$$

$$8. \int \frac{dx}{1+x^2} = \operatorname{arctg} x + C .$$

$$9. \int a^x dx = \frac{a^x}{\ln a} + C, a > 0, a \neq 1.$$

$$10. \int e^x dx = e^x + C .$$

$$11. \int \operatorname{tg} x dx = -\ln|\cos x| + C .$$

$$12. \int \operatorname{ctg} x dx = \ln|\sin x| + C .$$

$$13. \int \frac{dx}{\sin x} = \ln |\operatorname{cosec} x - \operatorname{ctg} x| + C = \ln \left| \operatorname{tg} \frac{x}{2} \right| + C .$$

$$14. \int \frac{dx}{\cos x} = \ln |\sec x + \operatorname{tg} x| + C = \ln \left| \operatorname{tg} \left(\frac{x}{2} + \frac{\pi}{4} \right) \right| + C .$$

$$15. \int \frac{dx}{a^2 + x^2} = \frac{1}{a} \operatorname{arctg} \frac{x}{a} + C, a \neq 0.$$

$$16. \int \frac{dx}{a^2 - x^2} = \frac{1}{2a} \ln \left| \frac{a+x}{a-x} \right| + C, a \neq 0.$$

$$17. \int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \ln \left| \frac{x-a}{x+a} \right| + C, a \neq 0.$$

$$18. \int \frac{dx}{\sqrt{a^2 - x^2}} = \arcsin \frac{x}{a} + C, |x| < a, a \neq 0.$$

$$19. \int \frac{dx}{\sqrt{x^2 \pm a^2}} = \ln \left| x + \sqrt{x^2 \pm a^2} \right| + C .$$

$$20. \int \sqrt{x^2 + a^2} dx = \frac{x}{2} \sqrt{x^2 + a^2} + \frac{a^2}{2} \ln \left| x + \sqrt{x^2 + a^2} \right| + C .$$

$$21. \int \sqrt{x^2 - a^2} dx = \frac{x}{2} \sqrt{x^2 - a^2} - \frac{a^2}{2} \ln \left| x + \sqrt{x^2 - a^2} \right| + C .$$