

Tasks. A straight line and a plane in a space

1. Form an equation of a plane passing through the point $M(3, -2, -7)$ and parallel to the plane $2x - 3z + 5 = 0$.

2. Form an equation of a plane passing through the point $M(3, -1, 2)$ and perpendicular to two given planes $3x + y - z + 2 = 0$ and $x + 4z + 1 = 0$.

3. Form an equation of a plane perpendicular to the plane $2x - 2y + 4z - 5 = 0$ and cut on the coordinate axes OX and OY two segments $a = -2$ and $b = 2/3$.

4. Find the distance between the following parallel planes $x - 2y + 3z + 7 = 0$ and $x - 2y + 3z - 1 = 0$.

5. Write down canonical equations of the straight line
$$\begin{cases} x - y + 3z - 1 = 0 \\ 2x + y + z - 2 = 0 \end{cases}$$

6. Form an equation of a straight line passing through the point $M(3, -2, -7)$ and perpendicular to the plane $2x - 3z + 5 = 0$.

7. The apexes $A(2, 3, 4)$, $B(4, 7, 3)$, $C(1, 2, 2)$ and $D(-2, 0, 1)$ are given. Find: 1) the straight line and the length of its edge AB ; 2) an angle between the straight lines AB and CD ; 3) an equation of the plane ABC ; 4) an equation of the altitude dropped from the apex D on the plane ABC ; 5) an angle between the straight line AD and the plane ABC .

8. At which value of m the straight line $\frac{x+1}{3} = \frac{y-2}{m} = \frac{z+3}{-2}$ is parallel to the plane $x - 3y + 6z + 7 = 0$?

9. Find at what values of λ and μ the couple of equations will define parallel planes
$$\begin{cases} (1) 2x + \lambda y + 3z - 5 = 0 \\ (2) \mu x - 6y - 6z + 2 = 0 \end{cases}$$

10. Find at what value of λ the couple of equations will define perpendicular planes (1) $5x + y - 3z + 3 = 0$ (2) $2x + \lambda y - 3z = 0$.